國立政治大學【應用數學系】104學年度第2學期學科考試試題

考試科目:【組合學】

系級:研究所

考試時間:105年03月07日(一)

下午1:00~4:00

■ 本試卷共有6題,

<u>碩士班:請選5題作答</u>,每題20分,請在答案卷最前面註明所選的5題,否則依學生作答 之前5題計分。

博士班:6題全作答,每題17分,超過100分,則以100分計。

- 1. Show that if G is a planar graph with r regions, e edges, v vertices, and c components, then r e + v c = 1.
- 2. Show that $\sum_{k=0}^{r} C_k^{n+k} = C_r^{n+r+1}$.
- 3. How many subsets of $\{1, 2, ..., n\}$ are there with no consecutive numbers?
- 4. How many binary trees are there with n leaves?
- 5. Let $A_1, A_2, ..., A_n \subseteq U$ and $I \subseteq \{1, 2, ..., n\}$. Show that $|\overline{A_1 \cup A_2 \cup \cdots \cup A_n}| = \sum_{k=0}^{n} (-1)^k \sum_{|I|=k} |\bigcap_{i \in I} A_i|$.
- 6. How many ways are there to 4-color the edges of a tetrahedron?

不可使用計算機!

命題教師簽名:

